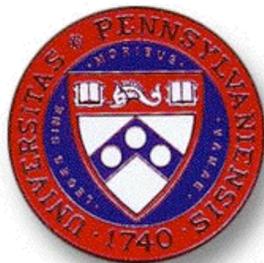


*Precision Measurements
of the Top Quark Mass
at the Tevatron*

DANIEL WHITESON

UNIVERSITY OF PENNSYLVANIA

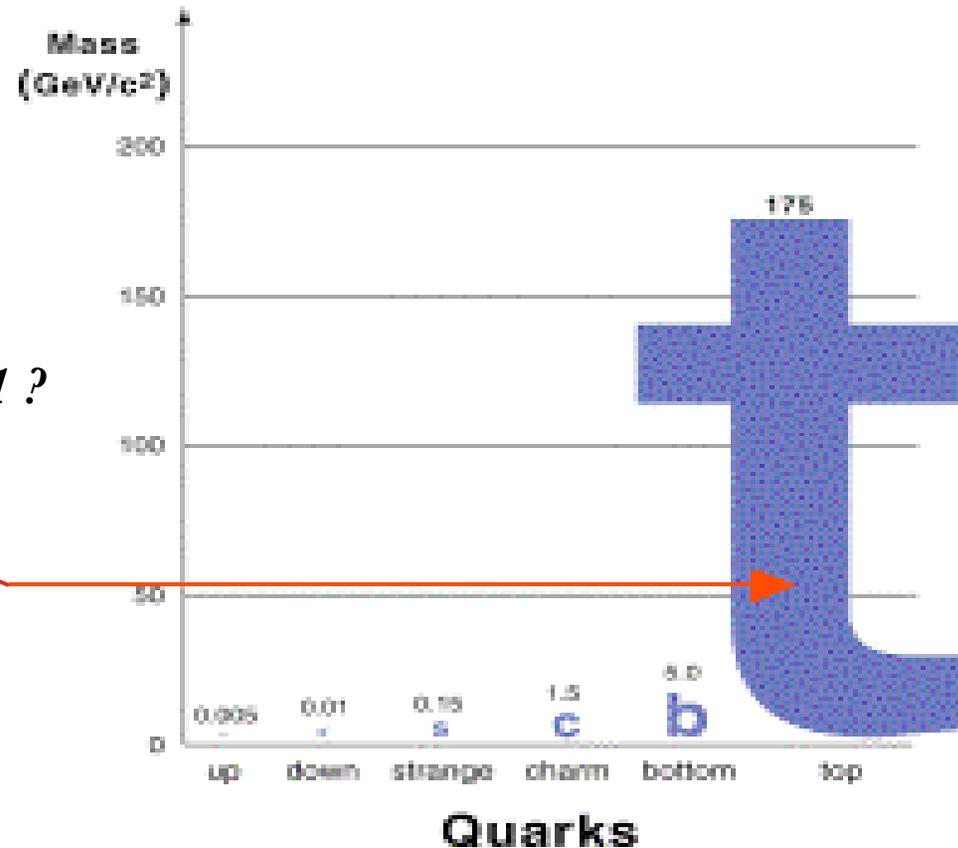
ON BEHALF OF THE CDF AND DZERO COLLABORATIONS



Top Quark

Where does this mass structure come from?
What does it reveal?
Why is the top so heavy?
Why is its Yukawa coupling ~ 1 ?

QUARK MASSES



Higgs

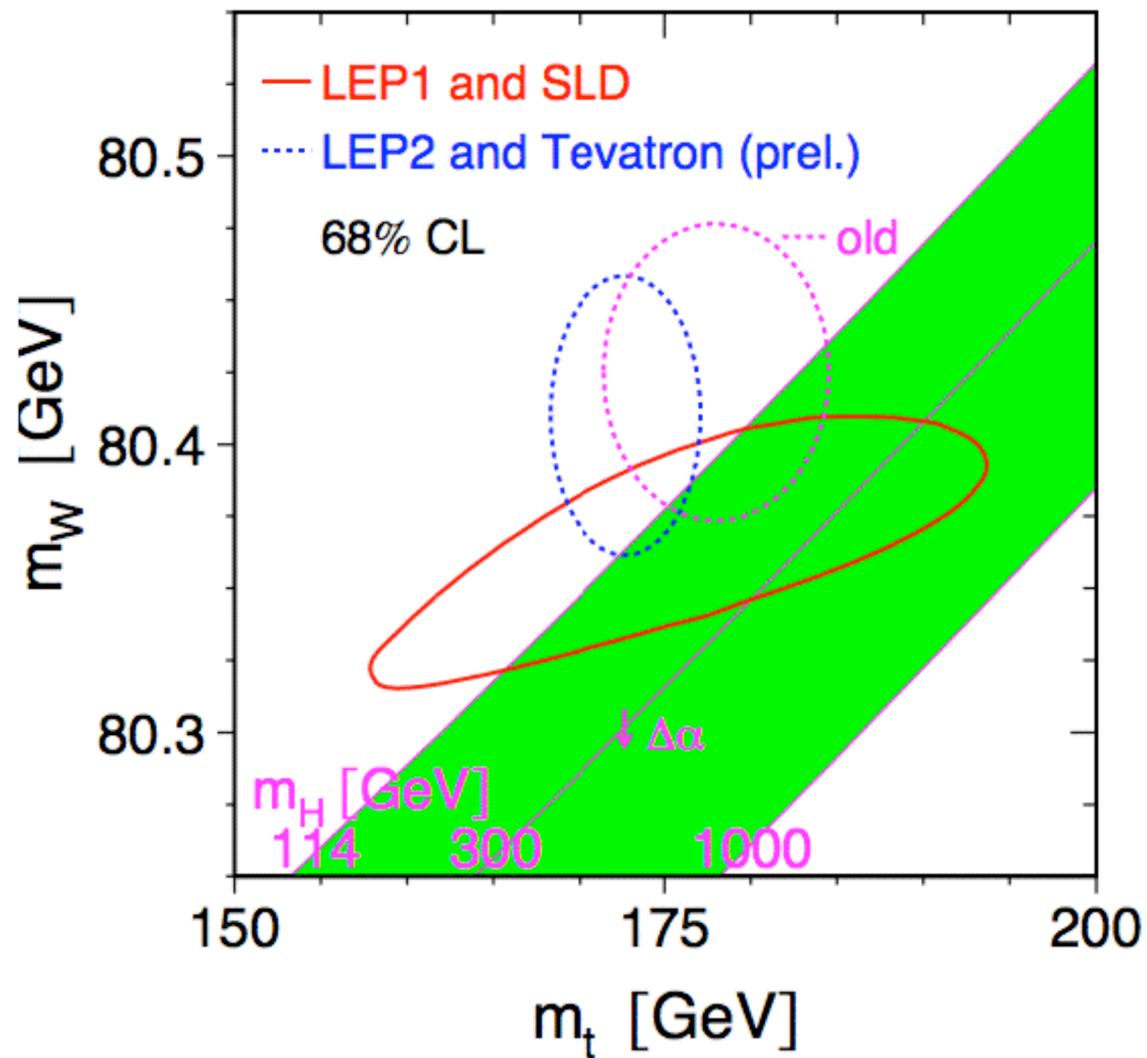
Update plot!

Higgs connection

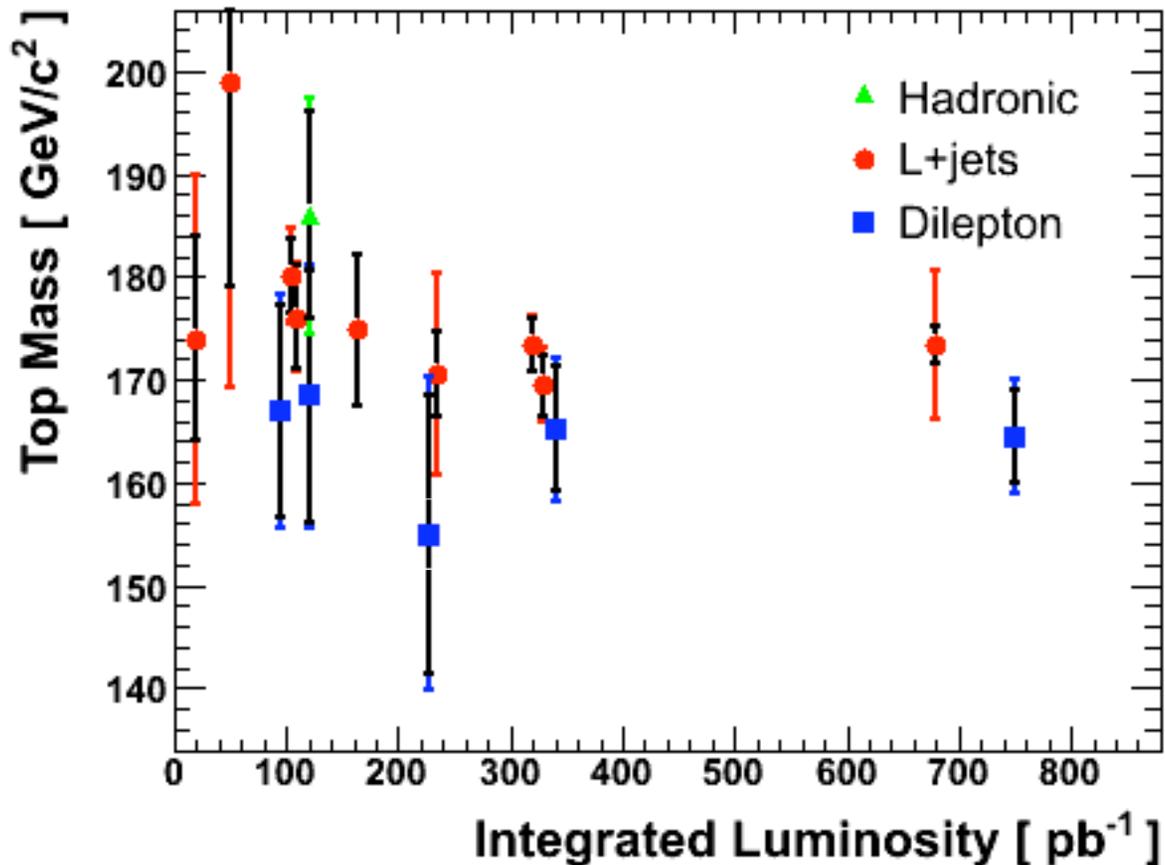
Radiative corrections

Heavy top means heavy Higgs

M_t provides constraints on M_h



Top measurements



L+jets error dominated by systematics!

Dilepton error will soon be systematics limited.

The future era will be devoted to systematic errors, and comparison among channels

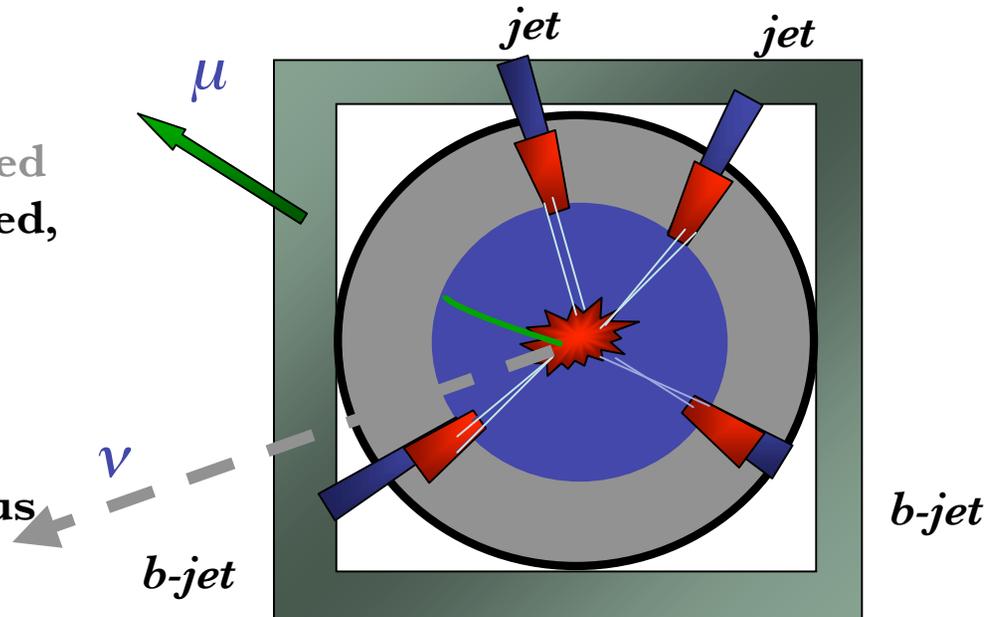
How to measure mass

How do we measure the mass?

Can't just put the pieces back together again

Lost information

- Neutrinos have escaped undetected
- Quarks have hadronized, showered, been clustered into *jets*
- Lepton resolution is **good**, but not perfect
- Assignment of reconstructed objects to partons is not obvious



Misinformation

- Background processes mimic top-ology

Solution

Lepton+jets

4 jet resolutions

Jet-parton assignments

24 (no b -tags)

12 (1 b -tag)

4 (2 b -tags)

1 missing neutrino

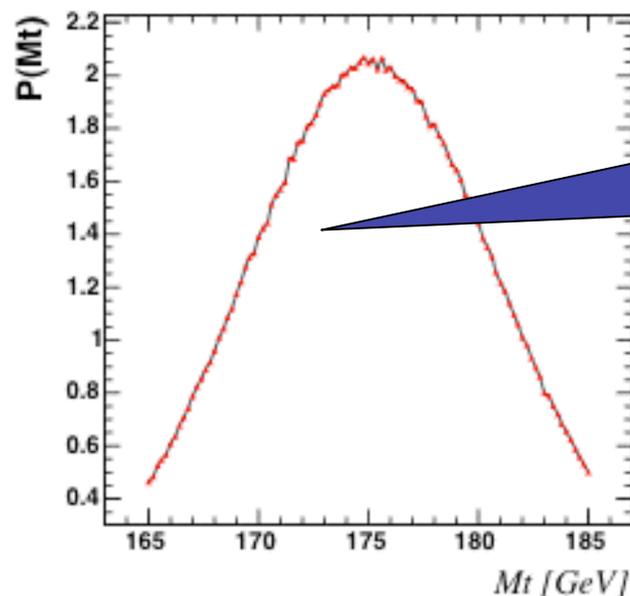
Dileptons

2 jet resolutions

Jet-parton assignments (2)

2 missing neutrinos

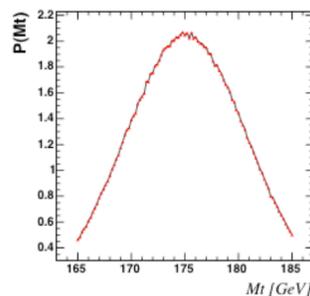
Monte Carlo integration over unmeasured quantities.



Construct probability curve $P(M_t)$ for each event.

Form joint probability for sample,
choose most probable value.

Probability calculation



Template strategy

Example: parameterize $P(M_t)$ in terms of event-level variable: **Reconstructed M_{top}**

Derive parameters from templates of simulated events.

Best measurement in *lepton+jets*

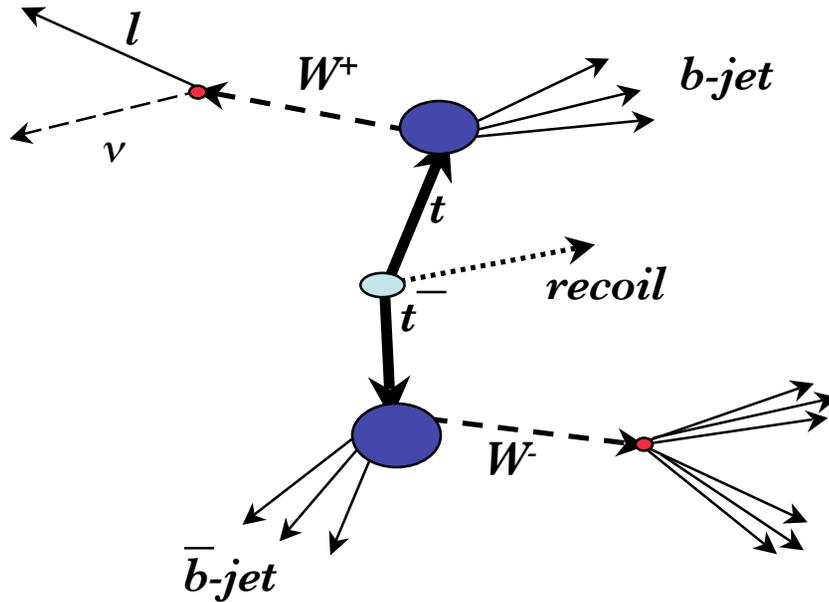
Matrix-element strategy

Calculate $P(M_t)$ directly for each event by convoluting matrix element with resolution functions.

Make simplifying approximations and measure corrections in simulated events.

Best measurement in *dileptons*.

Templates: extracting fitted masses



Constrain

P_T balance

$$M_{l\nu} = M_W$$

$$M_{jj} = M_W$$

$$M_{t1} = M_{t2}$$

Vary

24 jet-parton assignments

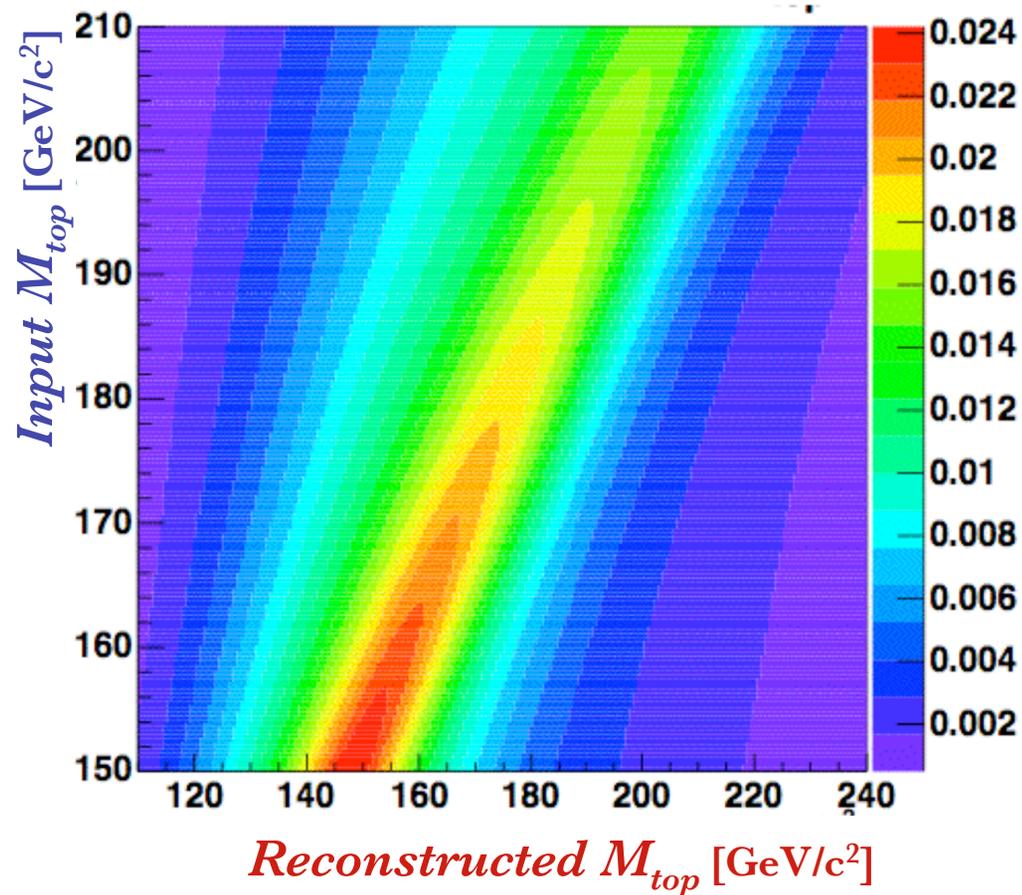
Measurements within resolutions

Reconstruct

Top mass (with best χ^2)

$$\chi^2 = \sum_{i=l,4 \text{ jets}} \frac{(p_T^{i,fit} - p_T^{i,meas})^2}{\sigma_i^2} + \sum_{j=x,y} \frac{(p_j^{UE,fit} - p_j^{UE,meas})^2}{\sigma_j^2} + \frac{(M_{jj} - M_W)^2}{\Gamma_W^2} + \frac{(M_{l\nu} - M_W)^2}{\Gamma_W^2} + \frac{(M_{bjj} - M_t)^2}{\Gamma_t^2} + \frac{(M_{bl\nu} - M_t)^2}{\Gamma_t^2}$$

Lepton+Jets template

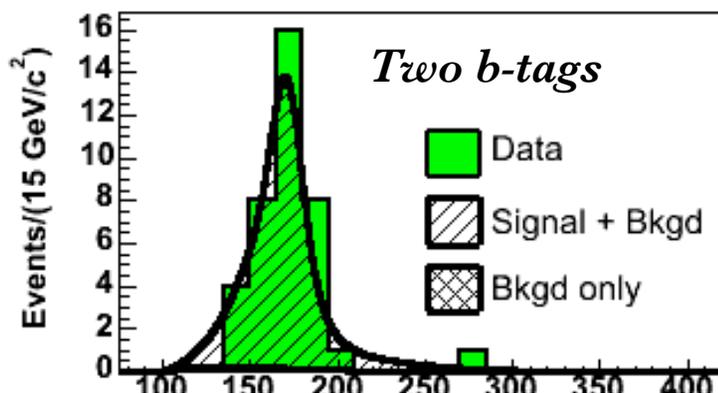


Reconstructed top mass is well correlated to **input** top mass.

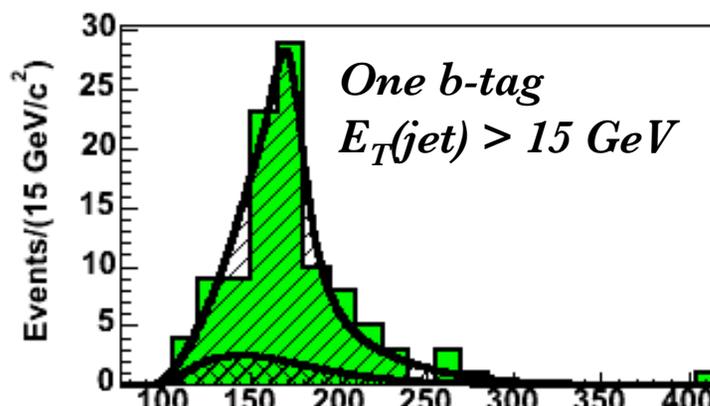
Lepton+jets

Reconstructed top mass in lepton + jets events

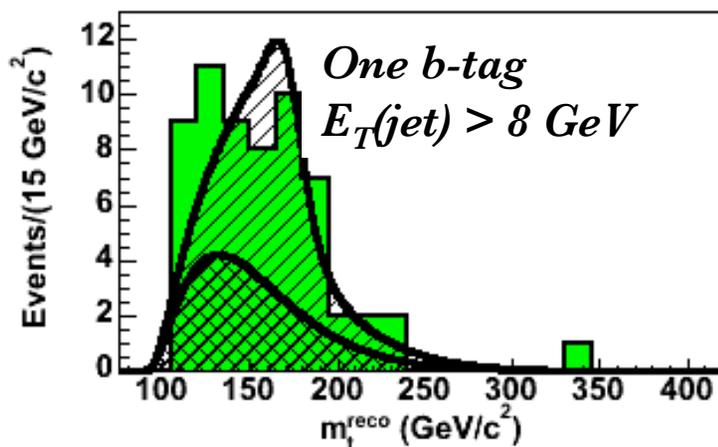
CDF Run II Preliminary (680 pb⁻¹)



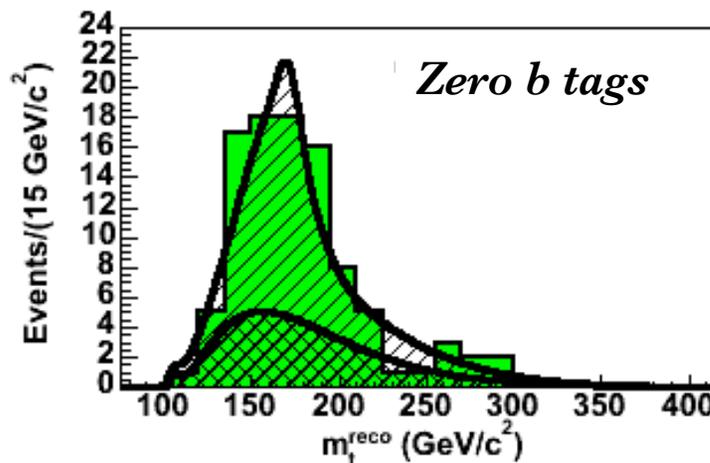
Reconstructed Top Mass [GeV/c²]



Reconstructed Top Mass [GeV/c²]

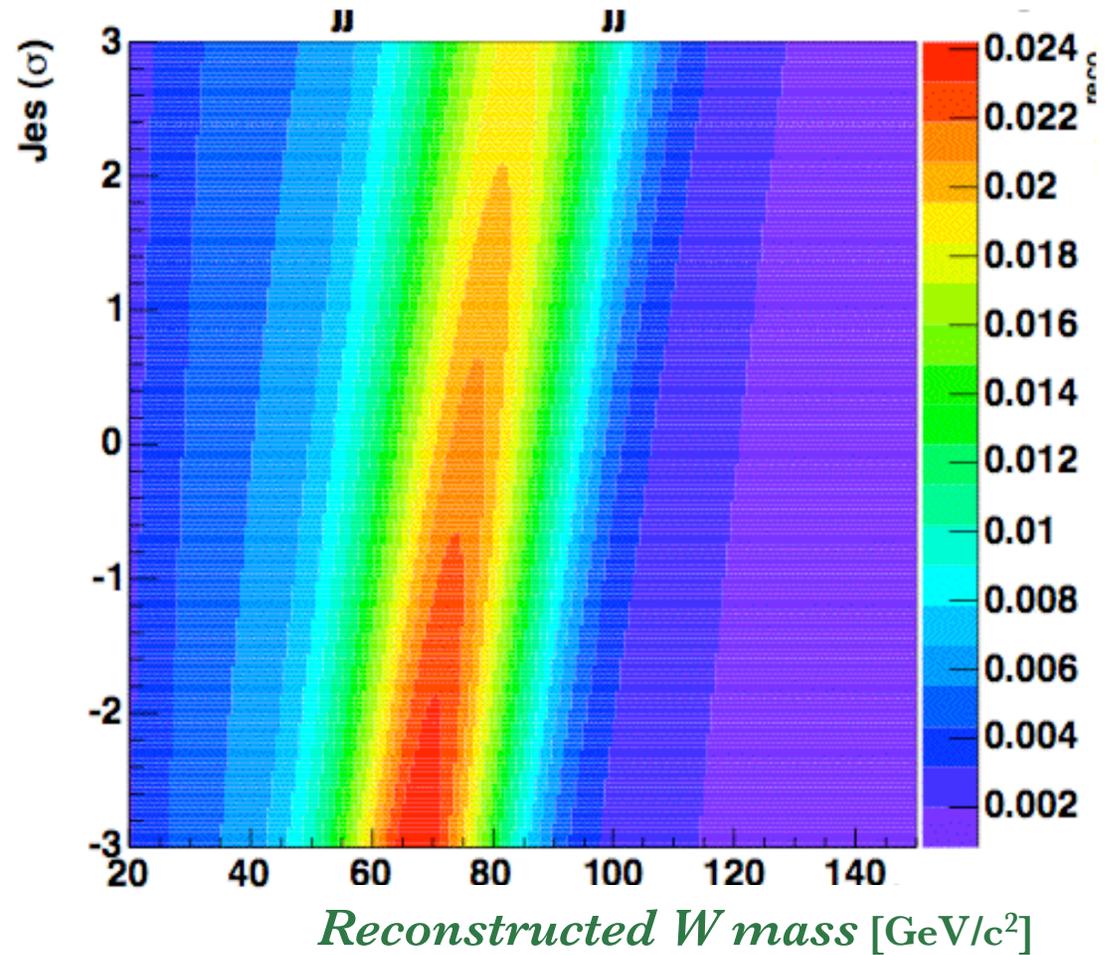
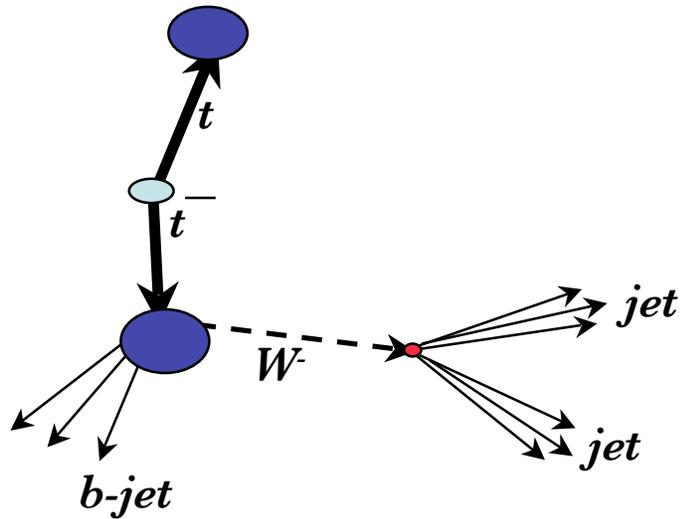


Reconstructed Top Mass [GeV/c²]



Reconstructed Top Mass [GeV/c²]

Reconstructed W mass

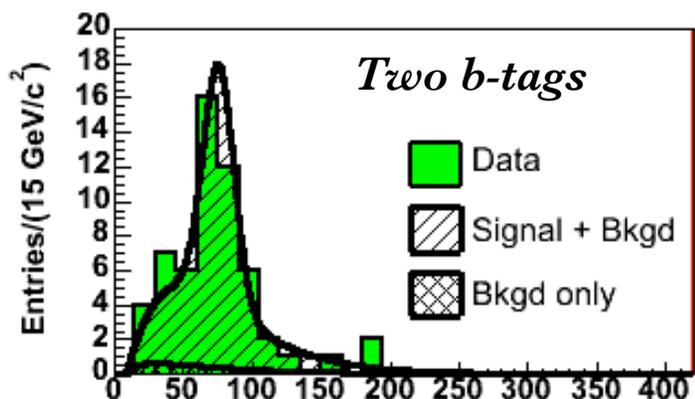


Reconstructed W mass is correlated to jet energy scale, expressed in units of $\sigma(P_T, \eta)$ from the external calibration.

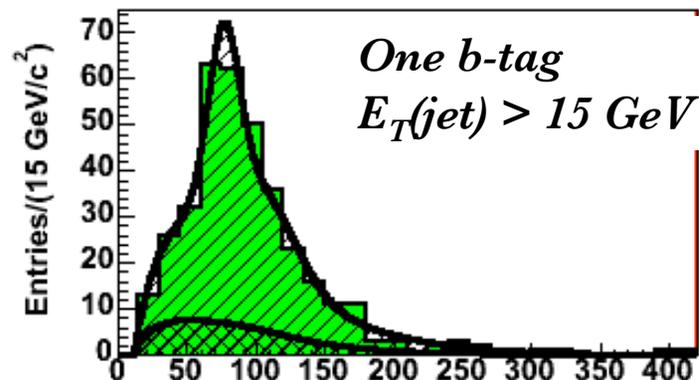
Lepton+Jets events

Reconstructed hadronic W mass in lepton + jets events

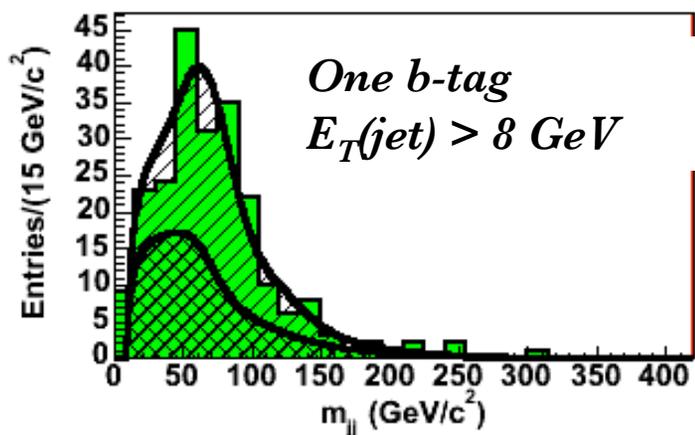
CDF Run II Preliminary (680 pb⁻¹)



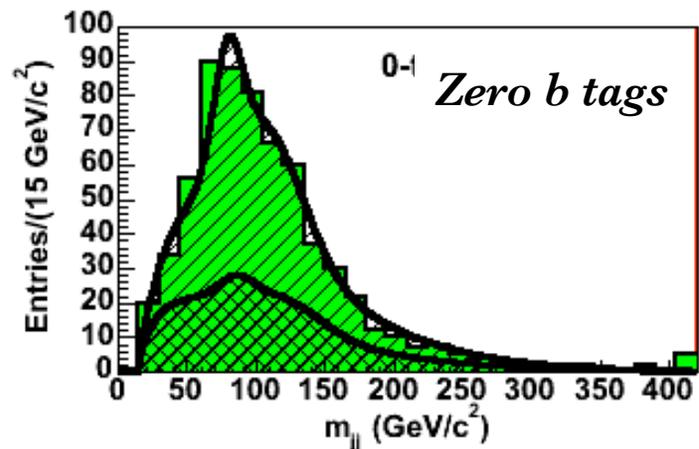
Reconstructed W Mass [GeV/c²]



Reconstructed W Mass [GeV/c²]

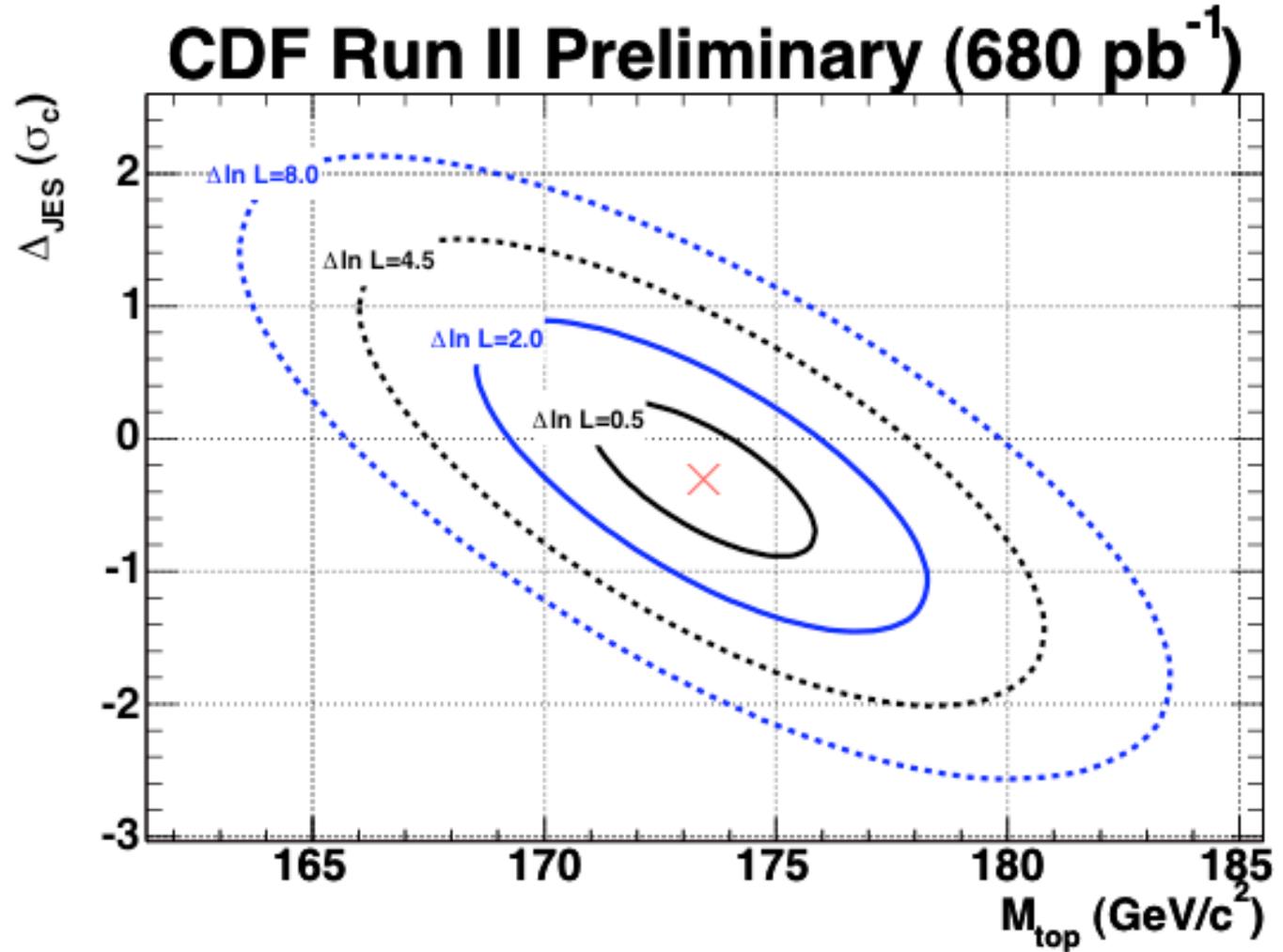


Reconstructed W Mass [GeV/c²]



Reconstructed W Mass [GeV/c²]

2D Likelihood



2D Result: $M_t = 173.4 \pm 1.7_{\text{(Stat)}} \pm 1.8_{\text{(JES)}} \pm 1.3_{\text{(syst)}} \text{ GeV/c}^2$
 $\Delta_{\text{JES}} = -0.3 \pm 0.6 \sigma$

Single best measurement of M_t . More precise than Run1!

Systematics

Systematics are largely due to uncertainties in modeling.

<i>Source</i>	$\Delta M_{top}(\text{GeV}/c^2)$
Remaining Jet Energy Scale	0.7
ISR/FSR	0.6
B-jet modeling	0.6
Background Shape	0.5
Background JES	0.4
Parton Distributions	0.3
Generator	0.2
Simulation Statistics	0.3
B-tagging	0.1
Total	1.3

Systematics

Systematics are largely due to uncertainties in modeling.

<i>Source</i>	$\Delta M_{top}(\text{GeV}/c^2)$
Remaining Jet Energy Scale	0.7
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Background Shape	0.5
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Simulation Statistics	0.3
B-tagging	0.1
Total	1.3

*From p_T and η dependence
of modeling uncertainties*

Systematics

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<i>Source</i>	$\Delta M_{top}(\text{GeV}/c^2)$
Remaining Jet Energy Scale	0.7
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Background Shape	0.5
Background JES	0.4
Parton Distributions	0.3
Generator	0.2
Simulation Statistics	0.3
B-tagging	0.1
Total	1.3

Model constrained by Z+jets data

Systematics

Systematics are largely due to uncertainties in modeling.

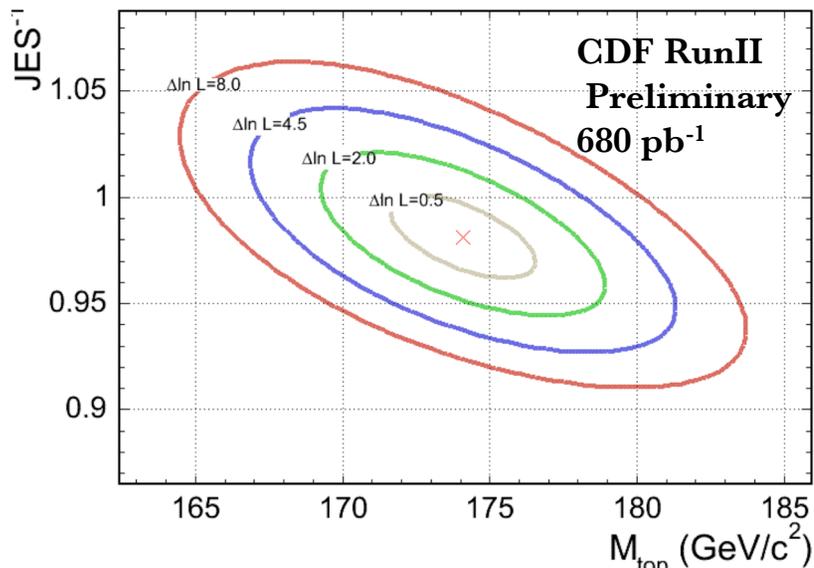
<i>Source</i>	$\Delta M_{top}(\text{GeV}/c^2)$
Remaining Jet Energy Scale	0.7
ISR/FSR	0.6
B-jet modeling	0.6
Background Shape	0.5
Background JES	0.4
Parton Distributions	0.3
Generator	0.2
Simulation Statistics	0.3
B-tagging	0.1
Total	1.3

*Uncertainties from
semi-leptonic decay,
fragmentation and
color flow.*

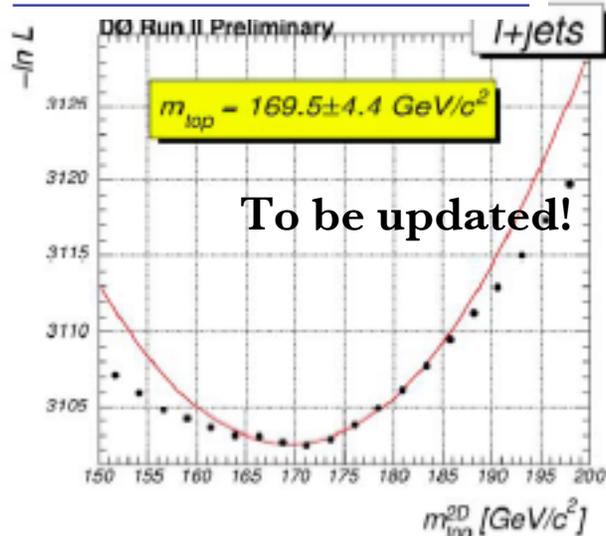
Other L+jets results

Add numbers to all.

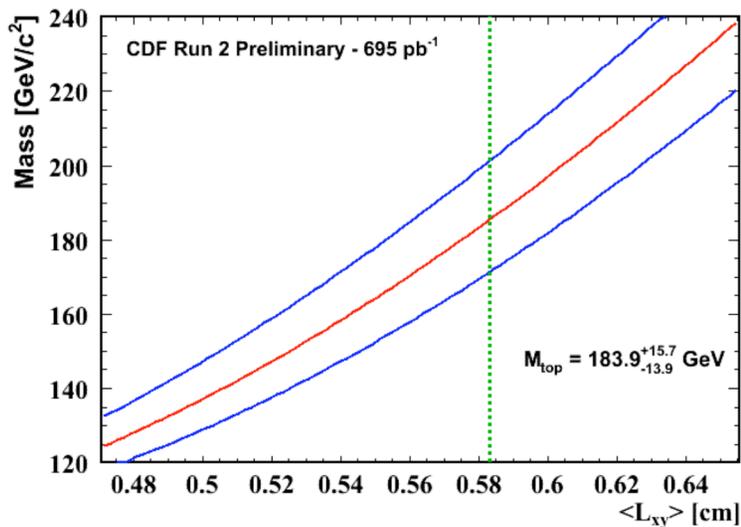
Matrix Element method



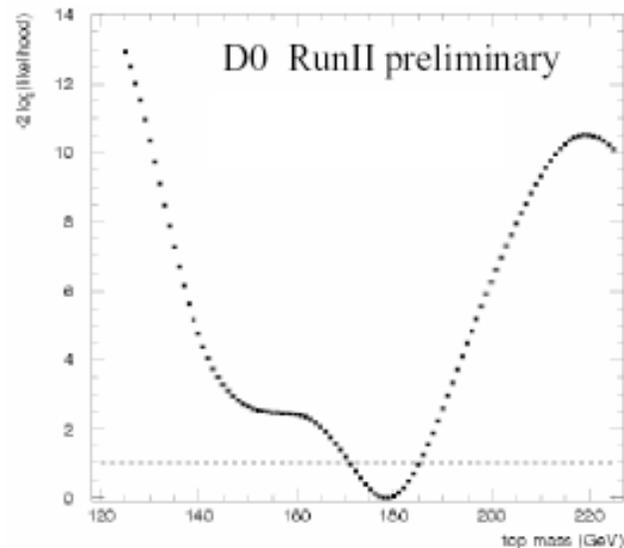
Matrix Element method



Transverse Decay Length of b



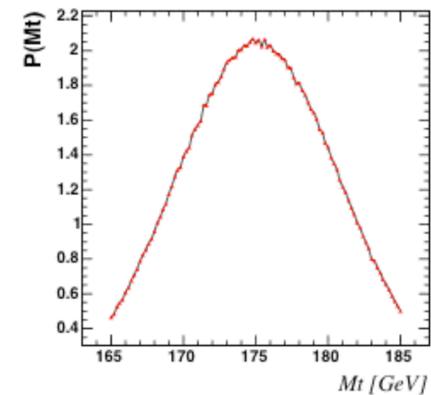
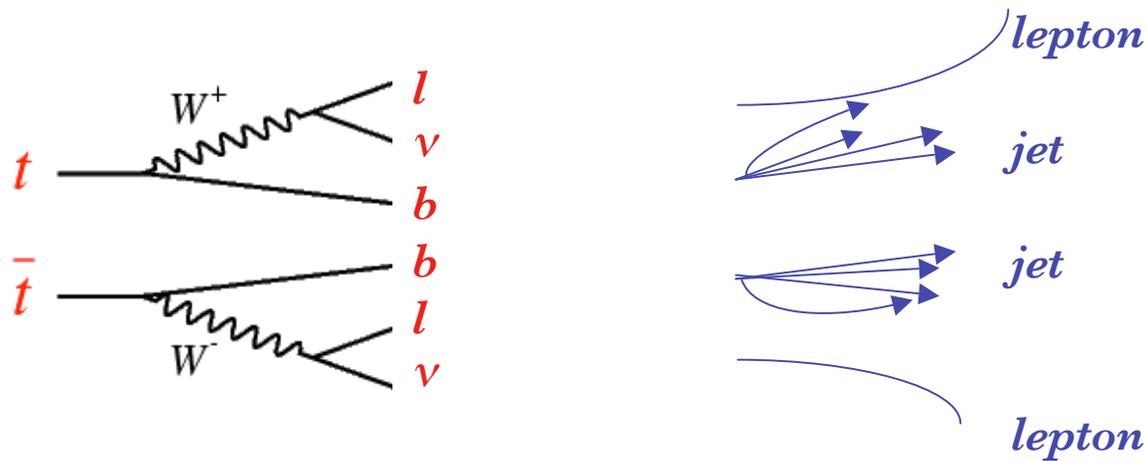
Ideogram method



Matrix Element Method
(as applied to dileptons)

Break into two pieces: parton-level process and showering/resolution effects

$$P(\text{partons} \mid M_t) \quad \times \quad P(\text{event } x \mid \text{partons}) \quad = \quad P(\text{event } x \mid M_t)$$



Integrate over 6 variables

- 2 Top masses
- 2 W masses
- 2 b-quark energies

Matrix Element method

$$P(\text{event } \mathbf{x} \mid \mathbf{M}_t) :$$

Differential cross-section calculation:

$$\frac{d\sigma(M_t)}{d\mathbf{x}} = \int d\Phi_6 |\mathcal{M}_{t\bar{t}}(p; M_t)|^2 \prod_{\text{jets}} f(p_i, j_i) f_{PDF}(q_1) f_{PDF}(q_2)$$

Phase-space
Integral

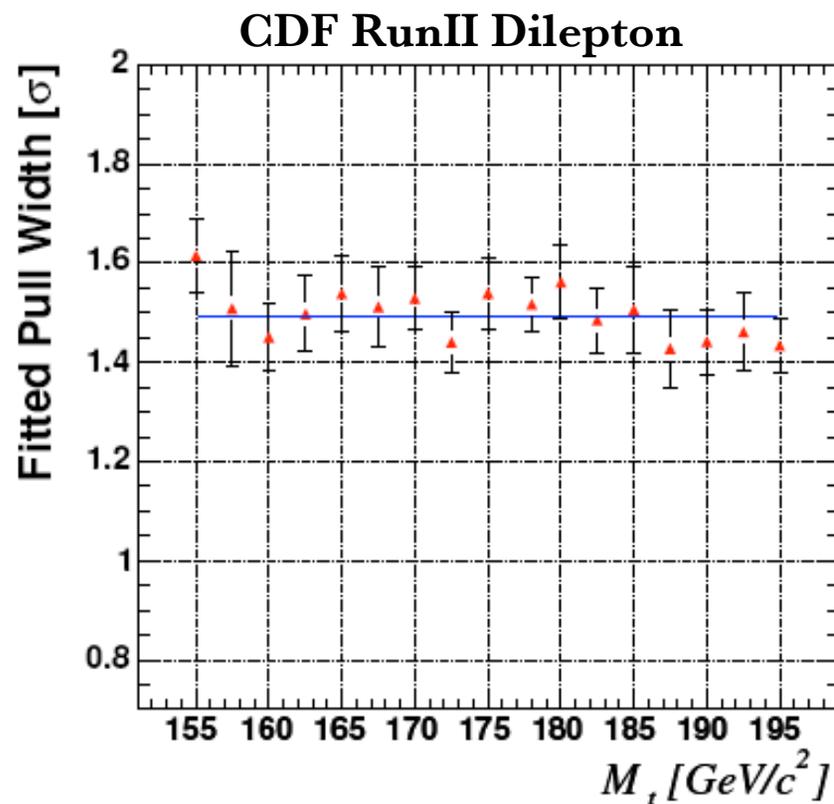
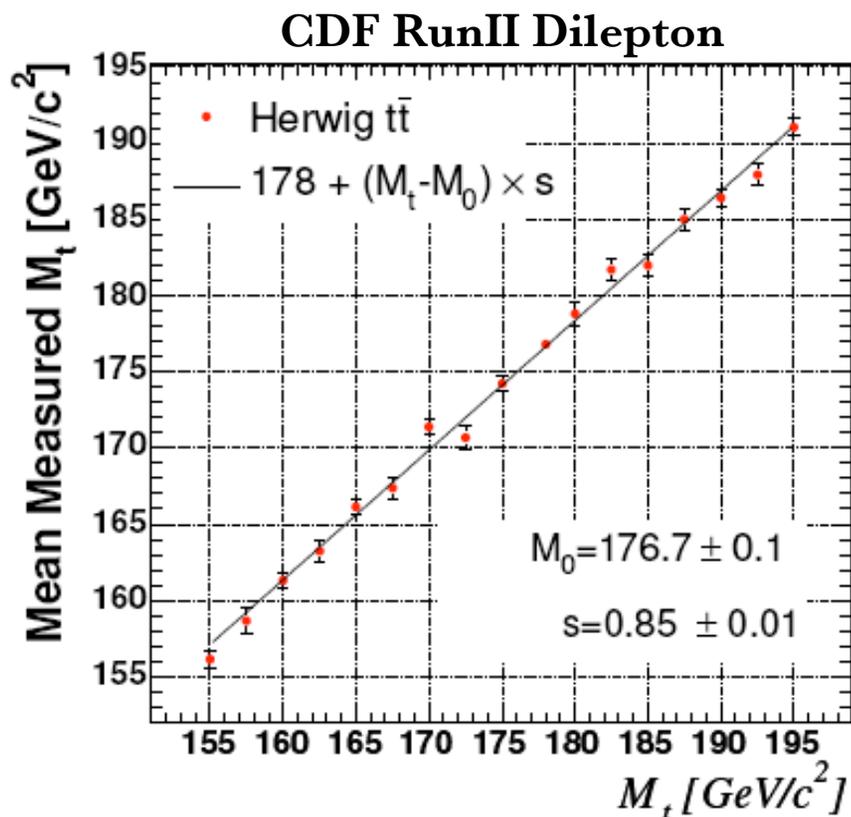
Matrix Element
 $P(\text{partons} \mid M_t)$

Transfer Functions
 $P(\text{event } \mathbf{x} \mid \text{partons})$

p 4-momentum of final partons
 q 4-momentum of initial partons
 \mathbf{x} measured event variables

Simulation Calibration: CDF RunII Dilepton

Approximations in calculation require calibration in simulation.



Response

Linear.

Slope < 1 due to backgrounds.

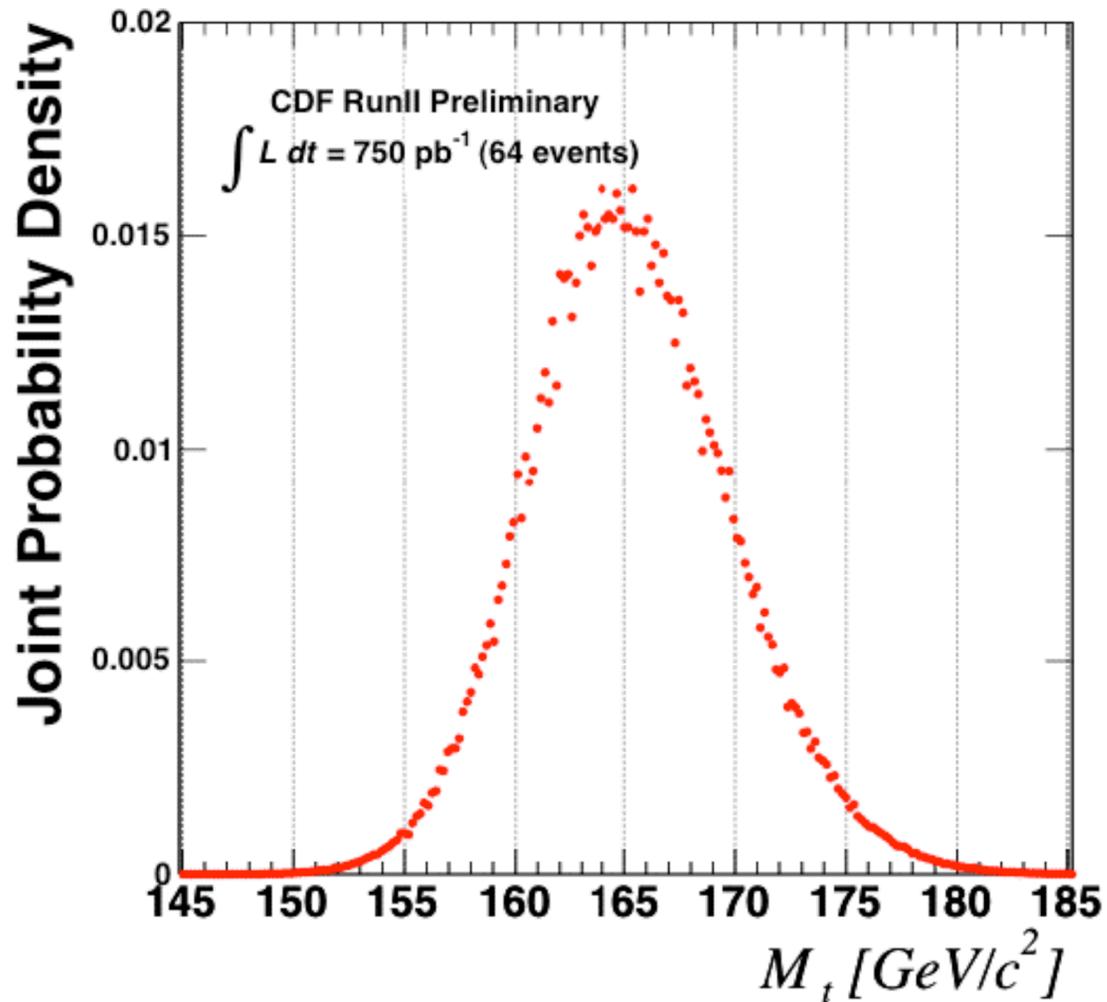
Pull width

Flat.

Pulls > 1 due to approximations made in $P(M_t)$ calculation.

Measurement!

*Most precise
single dilepton
measurement
to date.*



$$M_t = 164.6 \pm 4.5_{stat} \pm 3.1_{syst} \text{ GeV}/c^2$$

$$b\text{-tagged: } M_t = 162.7 \pm 4.6_{stat} \pm 3.0_{syst} \text{ GeV}/c^2$$

Systematic Errors

<i>Source</i>	$\Delta M_{top}(\text{GeV}/c^2)$
Jet Energy Scale	2.6
Background Statistics	0.8
Background Shape	0.8
ISR/FSR	0.7
Sample Composition	0.7
Parton Distributions	0.6
Generator	0.5
Method	0.3
Total	3.1

Systematic Errors

<i>Source</i>	$\Delta M_{top}(GeV/c^2)$	
Jet Energy Scale	2.6	<i>Could include $W \rightarrow jj$ calibration, but adds nothing to knowledge of M_t.</i> <i>Will include calibration from $Z \rightarrow bb$ and $\gamma + b$</i>
Background Statistics	0.8	
Background Shape	0.8	
ISR/FSR	0.7	
Sample Composition	0.7	
Parton Distributions	0.6	
Generator	0.5	
Method	0.3	
Total	3.1	

Systematic Errors

<i>Source</i>	$\Delta M_{top}(\text{GeV}c^2)$
Jet Energy Scale	2.6
Background Statistics	0.8
Background Shape	0.8
ISR/FSR	0.7
Sample Composition	0.7
Parton Distributions	0.6
Generator	0.5
Method	0.3
Total	3.1

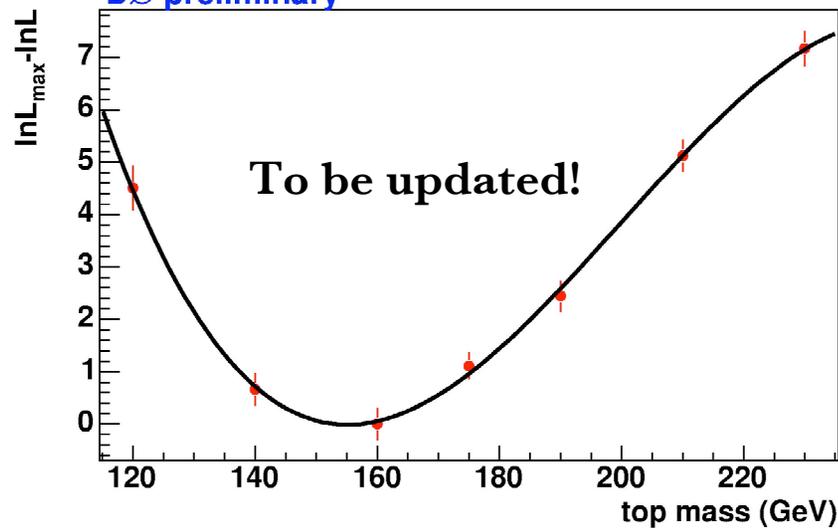
*Driven by small
sample of mis-ID
lepton candidates
drawn from data.*

Dilepton results

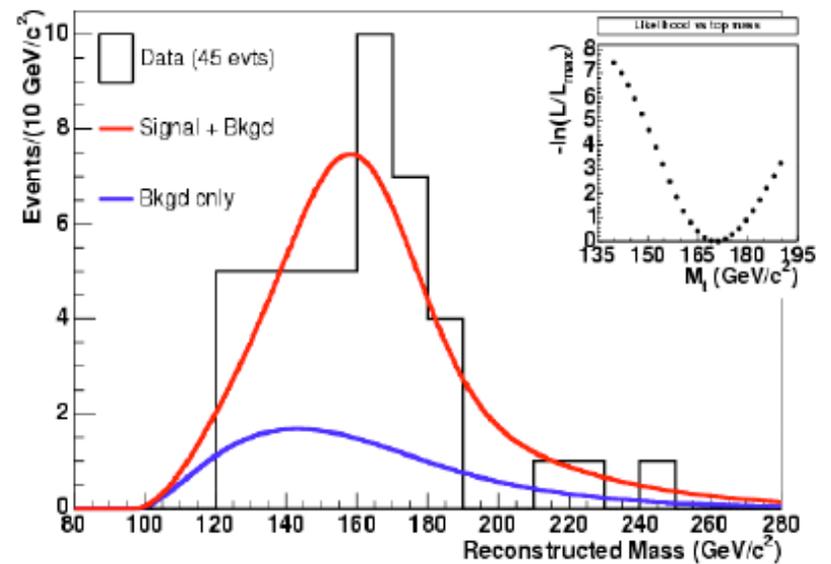
D0 Neutrino Weighting
Result 320pb-1 here

Matrix-Element Weighting

\emptyset preliminary

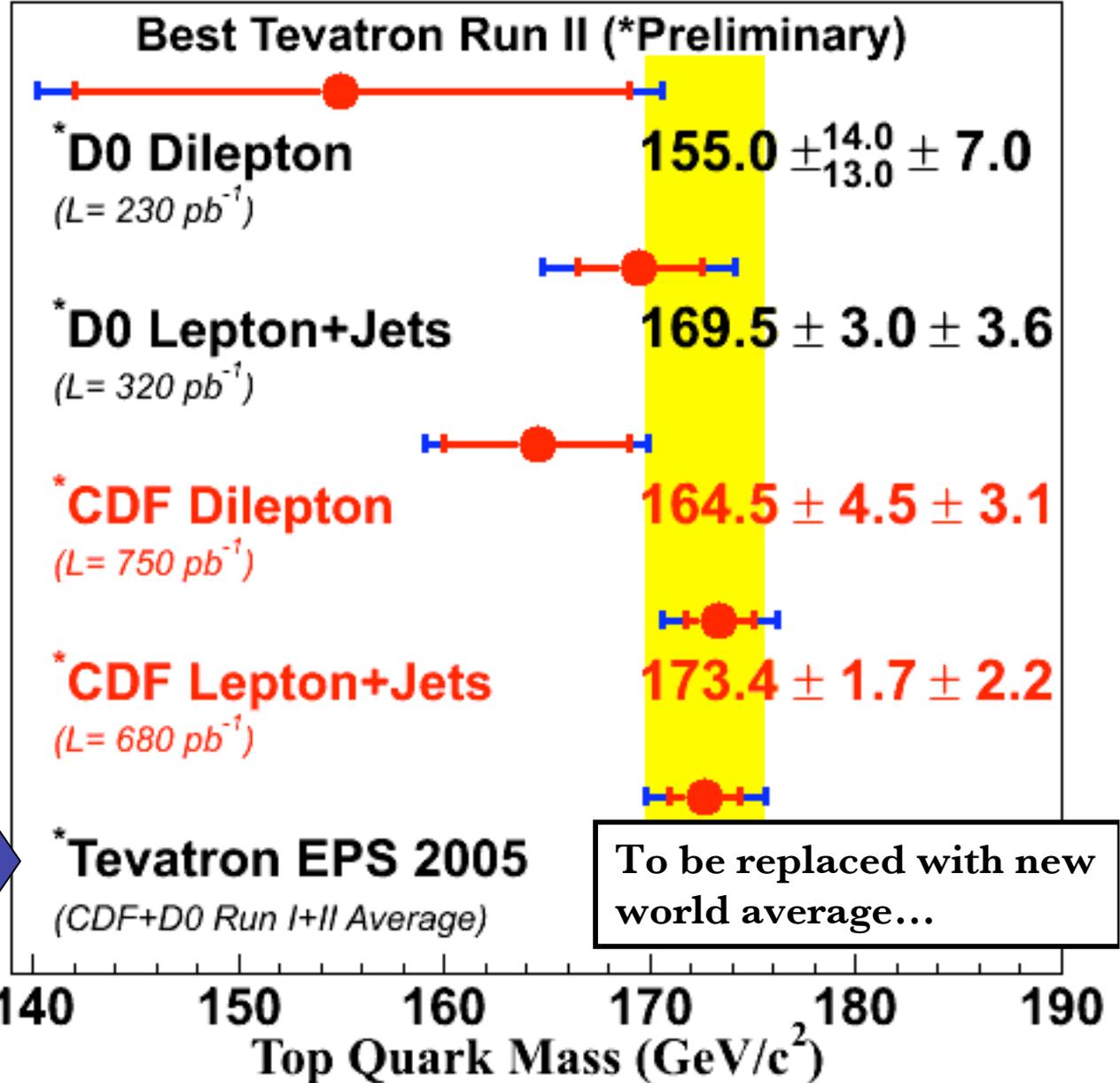


Neutrino Weighting Templates



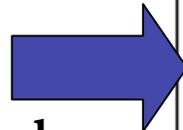
Impact

30



World Average

Total result has error of **2.4 GeV**, systematics limited.

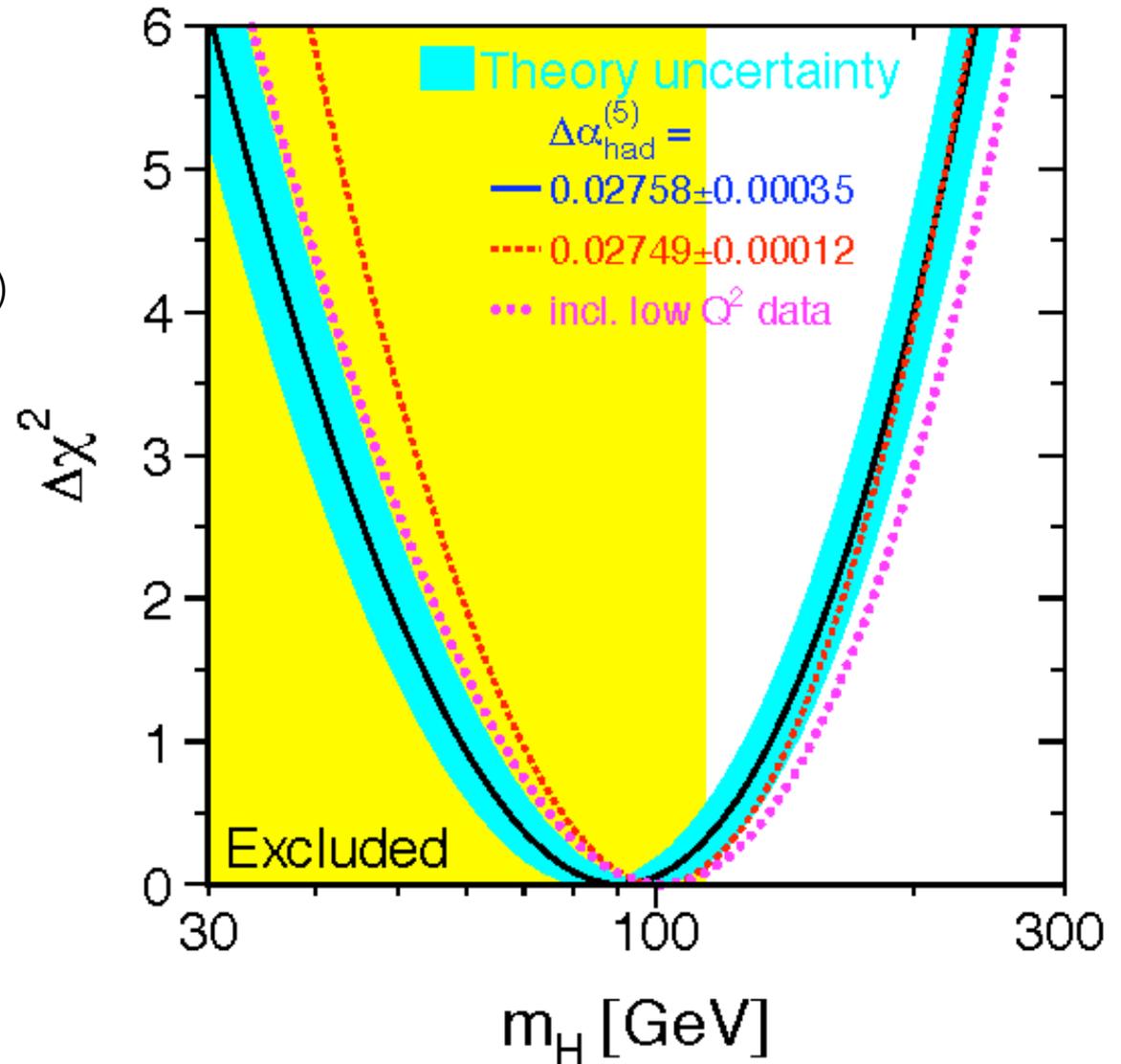


Higgs Impact

$$M_{\text{higgs}} = 91^{+45}_{-32} \text{ GeV}/c^2$$

$$M_{\text{higgs}} < 186 \text{ GeV}/c^2 \text{ (95\% conf)}$$

To be updated!

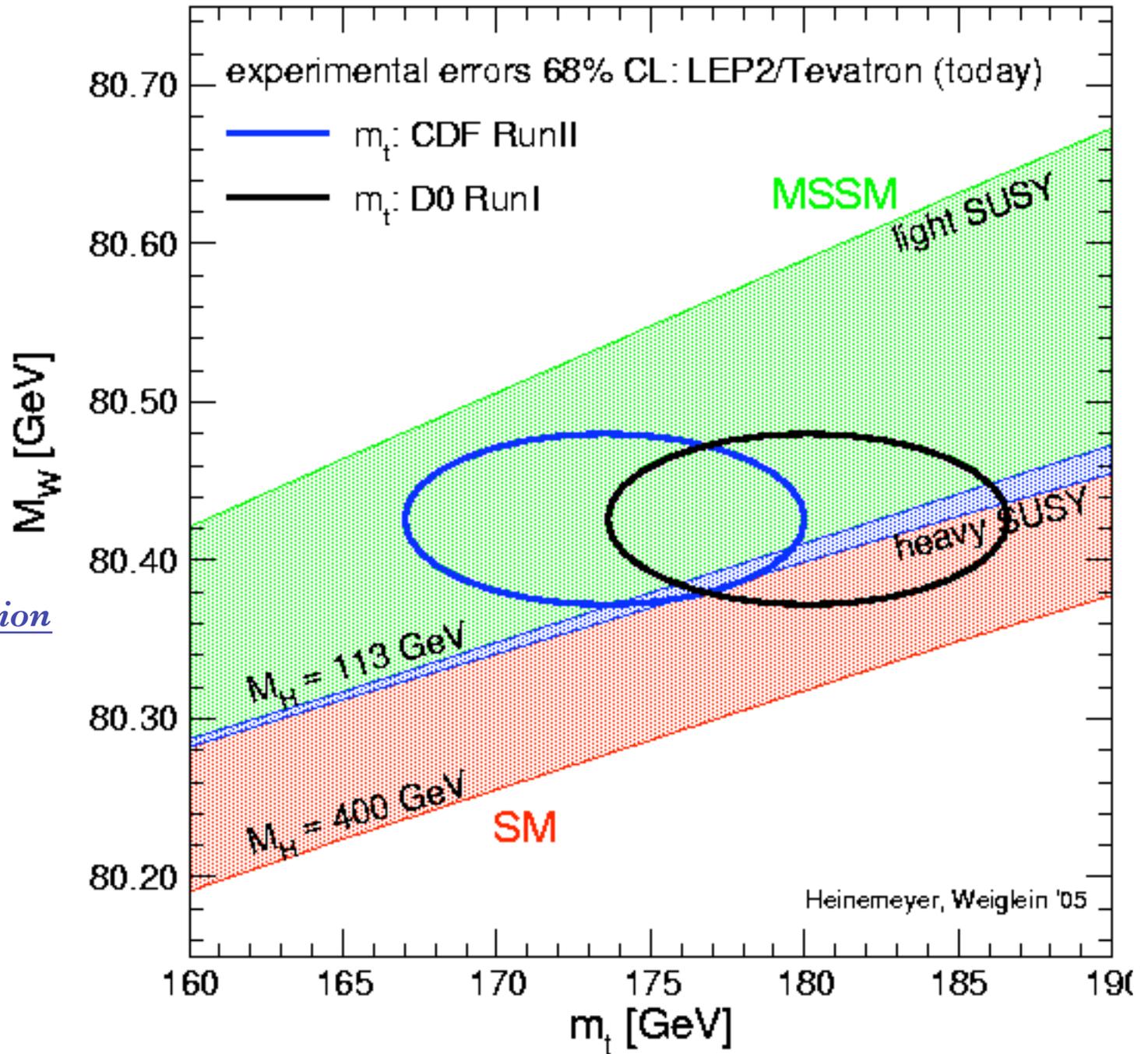


Impact of M_{top}

To be updated!

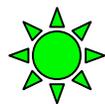
Improving precision

Precision M_{top}
affects SUSY
calculations.



Prospects for Systematics

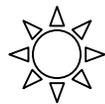
<i>Source</i>	<i>dilepton</i> $\Delta M_{top}(GeV/c^2)$	<i>l+jets</i> $\Delta M_{top}(GeV/c^2)$
Jet Energy Scale	2.6 	2.1 
Background Statistics	0.8 	0.3 
Parton Distributions	0.6 	0.3
Generator	0.5 	0.2
Background Shape	0.8 	0.5 
ISR/FSR	0.7 	0.6 
Sample Composition	0.7 	---
Method	0.3	---
B-tagging	---	0.1
Total	3.1	2.2



Improves with luminosity



More sophisticated treatments ahead



Improves with CPU time

Summary

Precision Measurement

Detector understanding leads
to precision results

We have measured the top
mass with an error of **< 3 GeV**

Dileptons & 1+jets consistent

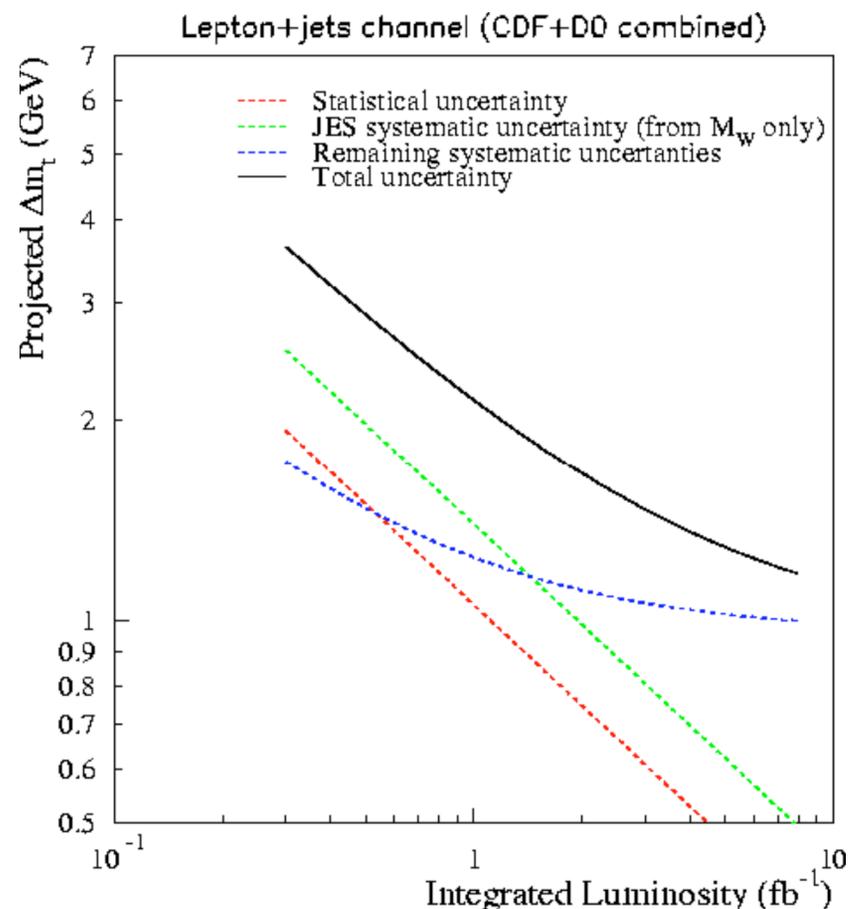
Room for Improvement

Systematic errors will decrease
All hadronic measurement in progress

Higher Precision Future

In **4fb⁻¹**,

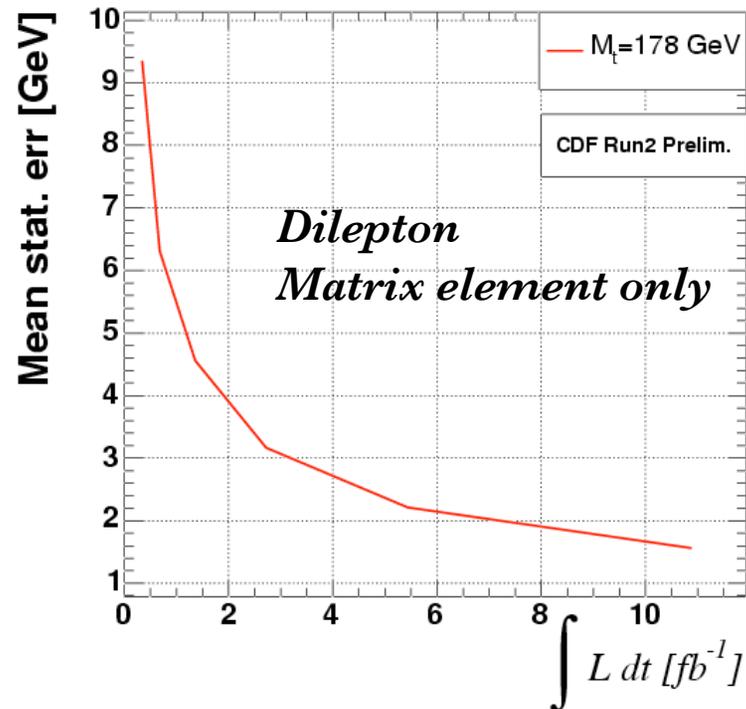
- expect **2 GeV** total error
 - Dileptons become systematics limited.
 - 1+jets and dileptons approach equal weight
 - Comparison of channels to test top hypothesis, look for new physics
- These results will be relevant for some years, even after LHC turn on*



Backup material

Prospects

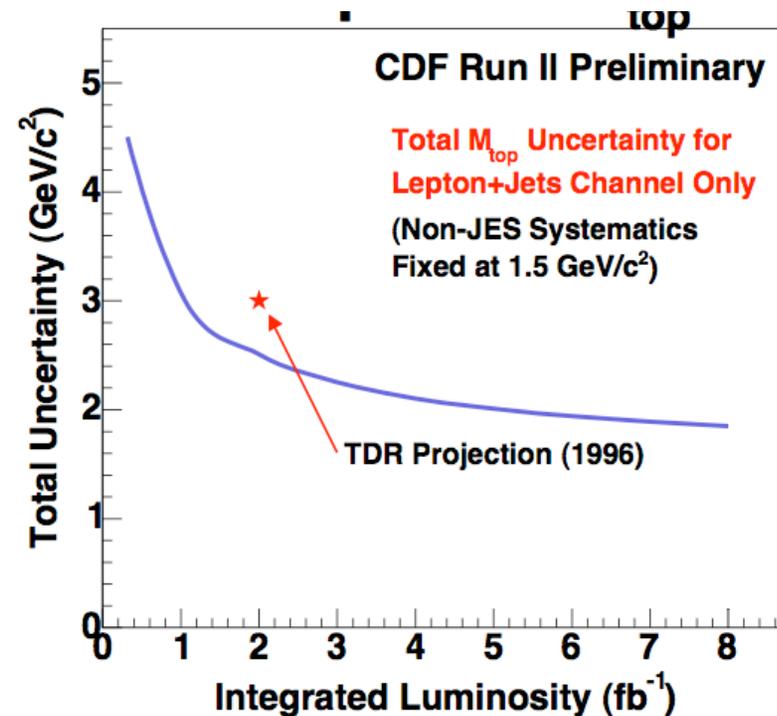
Dilepton Statistical Error



Dileptons

- Not yet systematics limited
(mean stat error of 2.5 GeV at 4fb⁻¹)
- Improved modelling of ISR
- Extract b-jet energy scale from $Z \rightarrow bb$

L+jets Total Error



L+jets

- Already systematics limited
- Data improves systematics ($W \rightarrow jj$)